## Cambridge O Level

## STATISTICS

4040/13
Paper 1
October/November 2022
MARK SCHEME
Maximum Mark: 100

## Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.
Cambridge International is publishing the mark schemes for the October/November 2022 series for most Cambridge IGCSE ${ }^{\text {TM }}$, Cambridge International A and AS Level components and some Cambridge O Level components.

## Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

## GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.


## GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

## GENERIC MARKING PRINCIPLE 3:

Marks must be awarded positively:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:
Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

## GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:
Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

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## MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

## Types of mark

M Method marks, awarded for a valid method applied to the problem.
A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.

B Mark for a correct result or statement independent of Method marks.
When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier, asterisked, mark in the scheme.

The symbol $\sqrt{ }$ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only.

## Abbreviations

| AG | answer given on question paper |
| :--- | :--- |
| awrt | answer which rounds to |
| cao | correct answer only |
| dep | dependent |
| ft | follow through after error |
| oe | or equivalent |
| SC | special case |
| soi | seen or implied |
| www | without wrong working |


| Question | Answer | Marks | Partial <br> Marks |
| :---: | :--- | ---: | :--- |
| 1 (a) | 10 | $\mathbf{1}$ | B1 |
| $1(\mathrm{~b})$ | 13 | $\mathbf{1}$ | B1 |
| 1 (c) | $29 / 35$ | $\mathbf{1}$ | B1 |


| Question | Answer | Marks | Partial <br> Marks |
| :---: | :--- | :--- | :--- |
| 2(a) | positive: as one variable increases, the other also increases or <br> variables in direct proportion | $\mathbf{2}$ | B1 |
|  | negative: as one variable increases, the other decreases <br> or variables in inverse proportion | B1 |  |
|  | A positive and B negative |  | B1 |
|  | A strong | B1 |  |
|  | B weak <br> if zero scored allow SC1 for linear positive for $A$ | B1 |  |
| 2(c) | eight scattered points showing no correlation | $\mathbf{1}$ | B1 |


| Question | Answer | Marks | Partial <br> Marks |
| :---: | :--- | ---: | :--- |
| 3(a) | the number of teenagers who like Hip-hop and Disco but not Rock | $\mathbf{1}$ | B1 |
| 3(b)(i) | 35 | $\mathbf{1}$ | B1 |
| 3(b)(ii) | 16 | $\mathbf{1}$ | B1 |
| 3(b)(iii) | 12 | $\mathbf{1}$ | B1 |
| 3(c) | $10+7(=17)$ or $9+7+10+14(=40)$ | $\mathbf{2}$ | M1 |
|  | $42.5[\%]$ | A1 |  |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 4(a)(i) | 9 | 1 | B1 |
| 4(a)(ii) | 32 | 1 | B1 |
| 4(a)(iii) | 13 | 1 | B1 |
| 4(b) | mid-point of 3-5 class is 4 | 3 | B1 |
|  | $\begin{aligned} & (20 \times 1)+(9 \times 2)+(5 \times \text { their } 4) \\ & \text { or }(2+3+4+6+5)+(2+4+6+4+2)+\text { their }(4+4+8+4+0) \end{aligned}$ |  | M1 |
|  | 58 |  | A1 |
| 4(c) | any valid reason, e.g. <br> number of dentists/doctors unknown, perhaps fewer dentists in the town than doctors, larger number of doctor visits could be shared around several doctors, <br> sample may not fairly represent whole town, sample size is small for a whole town | 1 | B1 |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 5(a) | 5 | 1 | B1 |
| 5(b) | any product of three probabilities with denominators 6 soi | 5 | M1 |
|  | five possible ways <br> $\begin{array}{lll}6 & 3 & 2 \\ 6 & 3 & 1\end{array}$ <br> $\begin{array}{lll}6 & 3 & 1 \\ 5 & 4 & 3\end{array}$ <br> $\begin{array}{lll}5 & 4 & 2\end{array}$ <br> 541 <br> any three identified with no incorrect extras soi <br> (allow M1 for one or two identified with no incorrect extras soi) |  | M2 |
|  | evidence of 6 cases for any correct way used |  | M1 |
|  | 30/216 or 5/36 |  | A1 |
| 5(c) | (their 5/36) ${ }^{2}$ | 2 | M1 |
|  | 25/1296 or 0.0193 ft |  | A1 $\sqrt{ }$ |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 6(a)(i) | Lizzy, range smallest | 1 | B1 |
| 6(a)(ii) | Emma, range largest | 1 | B1 |
| 6(a)(iii) | valid point relating to limitations of range as a measure of dispersion, e.g. <br> small/large range not a consequence of just one (or two) atypical journey(s) much shorter/longer than all the others, journey times evenly spread out, no extreme value(s) in journey times | 1 | B1 |
| 6(b)(i) | 398 | 1 | B1 |
| 6(b)(ii) | $(42.6 \times 10)-(36.2 \times 10)$ oe | 2 | M1 |
|  | 64 |  | A1 |
| 6(c) | longest journey time = shortest journey time + range for any worker implied by $41,4248,46$ or 47 seen | 2 | M1 |
|  | 7 |  | A1 |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 7(a) | attempted use of class mid-points $\left(\begin{array}{llllll} 21 & 23 & 25 & 27 & 29 & 31 \end{array}\right)$ | 7 | M1* |
|  | correct method for mean ( $\Sigma f x=1108$ ) dep |  | M1dep |
|  | 26.3-26.4 |  | A1 |
|  | finding values of $f \times$ variable squared |  | M1 |
|  | correct method for SD or variance ( $\left.\Sigma f x^{2}=29530\right)$ dep |  | M1dep |
|  | $2.67-2.69$ or $2.47-2.48$ |  | A1 |
|  | 26.4 and 2.67 |  | A1 |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 7(b) | [(their $\Sigma f x) \times 126 / 42] \div 12$ | 3 | M1 |
|  | 277 kg their $\Sigma \mathrm{fx} \div 4$ correct to 3sf ft |  | A1V |
|  | valid comment relating to milk production e.g. total amount of milk produced every 42 days stays the same, mean (for each 42 day period) unchanged, herd continues to produce milk at same rate as observed in the data |  | B1 |
| 7(c) | indication of column area proportional to class frequency, implied by non-standard frequencies of 6 or 14 or 5 or implied by calculating areas/counting squares | 5 | M1* |
|  | frequencies/areas/squares for profitable identified: $14 \quad 28 \quad 56$ |  | A1 |
|  | $5 \quad 1020$ |  | A1 |
|  | $[(14+5) / 30] \times 100 \text { or }[(28+10) / \text { their60 }]] \times 100$ or [(56 + 20)/their120] $\times 100$ dep |  | M1dep |
|  | 63.3[\%] |  | A1 |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 8(a) | $\begin{array}{lllllllll}25 & 43 & 54 & 62 & 68 & 73 & 77 & 80\end{array}$ | 1 | B1 |
| 8(b) | horizontal plots at UCBs | 3 | B1 |
|  | vertical plots at cfs |  | M1 |
|  | smooth curve through eight plotted points |  | A1 |
| 8(c)(i) | 0.87-0.93 | 1 | B1 |
| 8(c)(ii) | Q1: find magnitude for cf $=20(0.35-0.45)$ | 4 | M1 |
|  | Q3: find magnitude for cf $=60(1.80-1.90)$ |  | M1 |
|  | use $\mathrm{IQR}=\mathrm{Q} 3-\mathrm{Q} 1$ |  | M1 |
|  | 1.35-1.55 from correctly drawn graph |  | A1 |
| 8(d) | read magnitude for cf $=62+(0.45)(80-62)(=70.1)$ | 2 | M1 |
|  | $2.65-2.75$ |  | A1 |

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| Question | Answer | Marks | Partial <br> Marks |
| :---: | :--- | :--- | :--- |
| 8(e) | clear attempt to read magnitude for cf $=78$ |  | M1 |
|  | correct value from their correctly drawn graph | A1 |  |
| $8(\mathrm{f})$ | no/median better and valid reason | $\mathbf{2}$ | B1 |
|  |  | B1 |  |
|  | second valid reason <br> examples: <br> distribution is very unsymmetrical, <br> mean affected by the (relatively) few large values, <br> mean affected by extreme values, <br> more than half of values less than 1.0, <br> lots of values bunched at one end of the distribution |  |  |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 9(a) | correctly plotted points (allow B1 for 6 or 7 correct) | 2 | B2 |
| 9(b) | 3 | 1 | B1 |
| 9(c) | method for LSA $(5.3+5.4+5.5+5.6) / 4,(14+13+12+9) / 4$ | 3 | M1 |
|  | plot of $(5.45,12)$ |  | A1 |
|  | plot of (5.6125, 8.375) and (5.775, 4.75) |  | B1 |
| 9(d) | straight line through at least two of their plots in (c) | 4 | B1 |
|  | correct method for gradient |  | M1 |
|  | correct method for c using negative gradient |  | M1 |
|  | $m=-22.31$ to -22.30 and $c=133-134$ |  | A1 |
| 9(e) | put $y=1$ in their LOBF with negative $m$ and positive $c$ and find positive $x$ or <br> read $x$ from their graph with negative $m$ at $y=1$ | 2 | M1 |
|  | 5.94 mft |  | A1 $\sqrt{ }$ |
| 9(f) | valid explanation e.g. <br> linear relationship may not continue in extrapolated region, points scatter around line of best fit, extrapolation for only one person who could be completely atypical | 1 | B1 |


| Question | Answer | Marks | Partial <br> Marks |
| :---: | :--- | ---: | :--- |
| $9(\mathrm{~g})$ | 3 eliminated, selecting from 13 |  | B1 |
|  | $(3 / 13) \times(2 / 12)$ |  | M1 |
|  | $1 / 26$ |  | A1 |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 10(a) | 220/5.6 oe for any country | 3 | M1 |
|  | $39.3 \quad 38.7 \quad 62.6 \quad 27.8$ and C (allow A1 for all correct and incorrect choice or for three correct and correct choice or for non $1 d p$ values rounding correctly and $C$ ) |  | A2 |
| 10(b)(i) | $(160 / 360) \times 1780$ | 2 | M1 |
|  | 791 |  | A1 |
| 10(b)(ii) | $(90 / 360) \times 1780$ | 2 | M1 |
|  | 445 |  | A1 |
| 10(c) | [(84-60)/100] $\times 1780$ | 2 | M1 |
|  | 427 |  | A1 |
| 10(d) | $(35 / 100) \times 1780(=623)$ or $(95 / 360) \times 1780(\sim 470)$ | 4 | M1 |
|  | $(95 / 360) \times$ their 623 or $(35 / 100) \times$ their 470 |  | M1 |
|  | 164 or 165 |  | A1 |
|  | proportion of deaths by road user type same in South as in country as a whole |  | B1 |
| 10(e)(i) | death rates in different populations largely influenced by the age structure of the population | 1 | B1 |


| Question | Answer | Marks | Partial <br> Marks |
| :---: | :--- | ---: | ---: |
| 10 (e)(ii) | allow B1 for each of two relevant points <br> e.g. <br> for road accident death rates age may not be main determining <br> factor, <br> many other factors probably also relevant such as <br> traffic density in different places, <br> quality of roads, <br> whether place predominantly urban or rural, <br> general weather conditions in the places, <br> laws relating to road use, e.g. speed limits, <br> how experienced car drivers, cyclists etc are | B2 |  |

